



UCSG-NET - Unsupervised Discovering of Constructive Solid Geometry Tree



Wrocław University
of Science and Technology

Kacper Kania¹, Maciej Zieba^{1,2}, Tomasz Kajdanowicz¹

¹Wroclaw University of Science and Technology ²Tooploox

kacp.kania@gmail.com

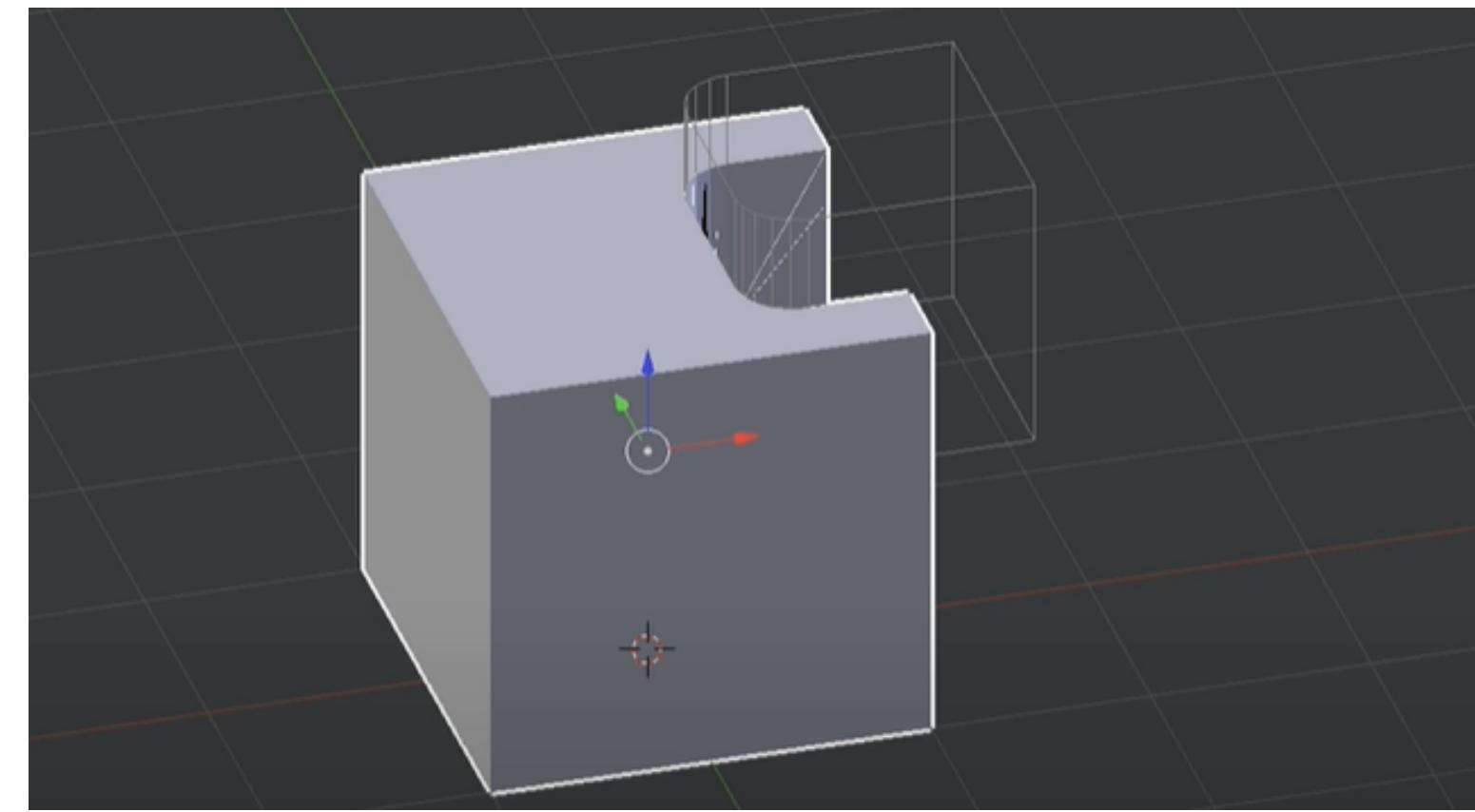


Contributions

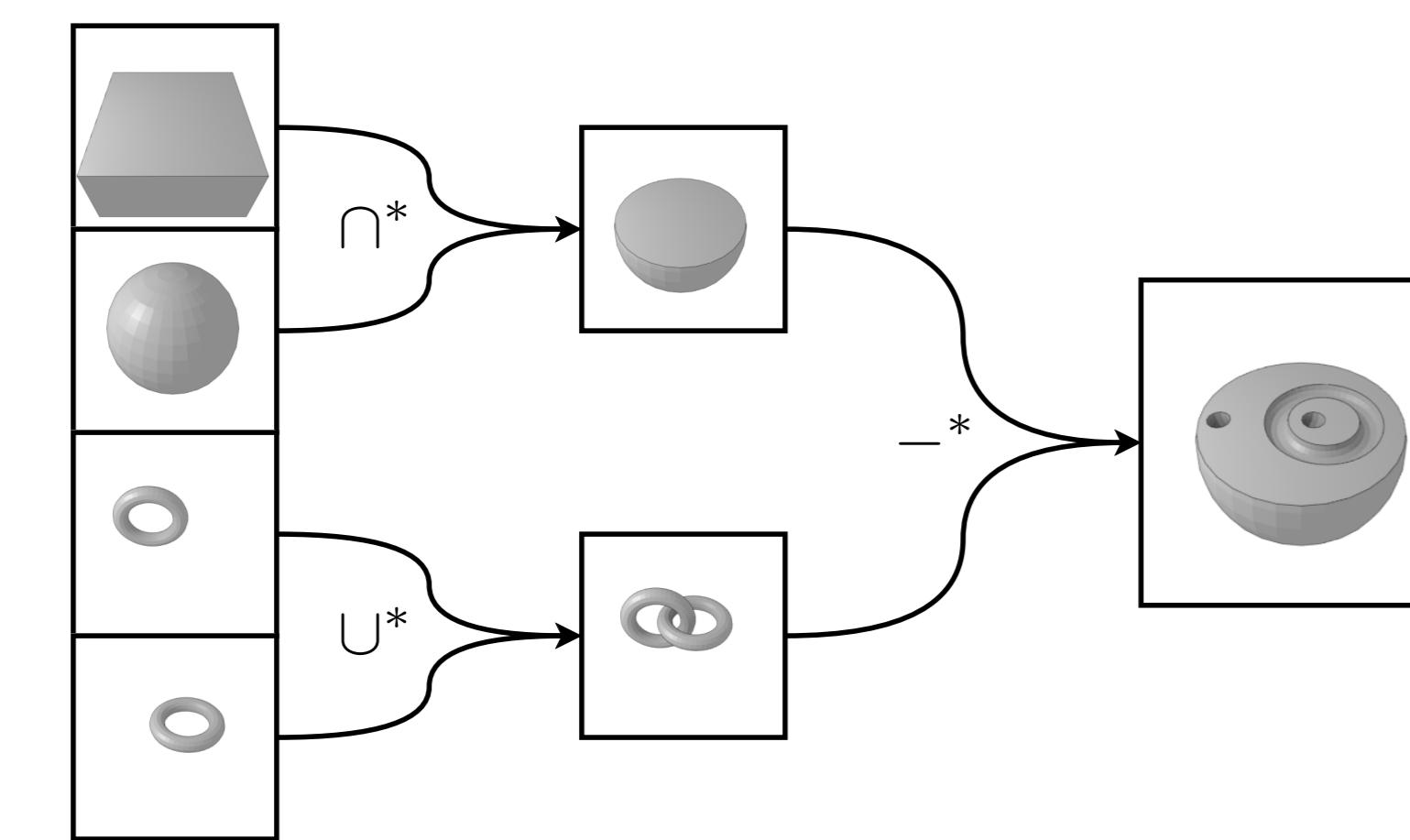
- The first method that learns CSG operations in **unsupervised manner**.
- Predicted CSG trees are fully **interpretable** and **controllable**. They can aid design of 3D objects.
- In terms of reconstruction quality, our model is **on par** with existing methods that aim for interpretable 3D object reconstruction.

Motivation

CSG is a common tool that can be in 3D graphics software for modeling objects with complex topology.

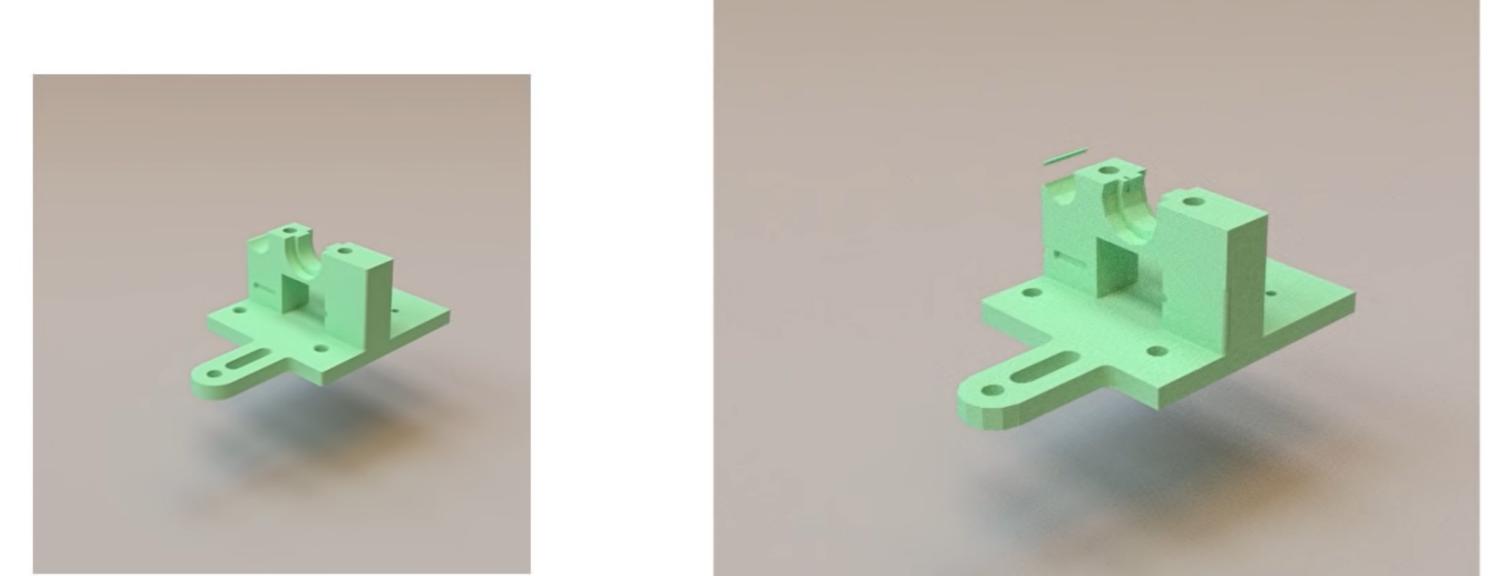


We aim to automate the process by predicting CSG trees that create these objects.



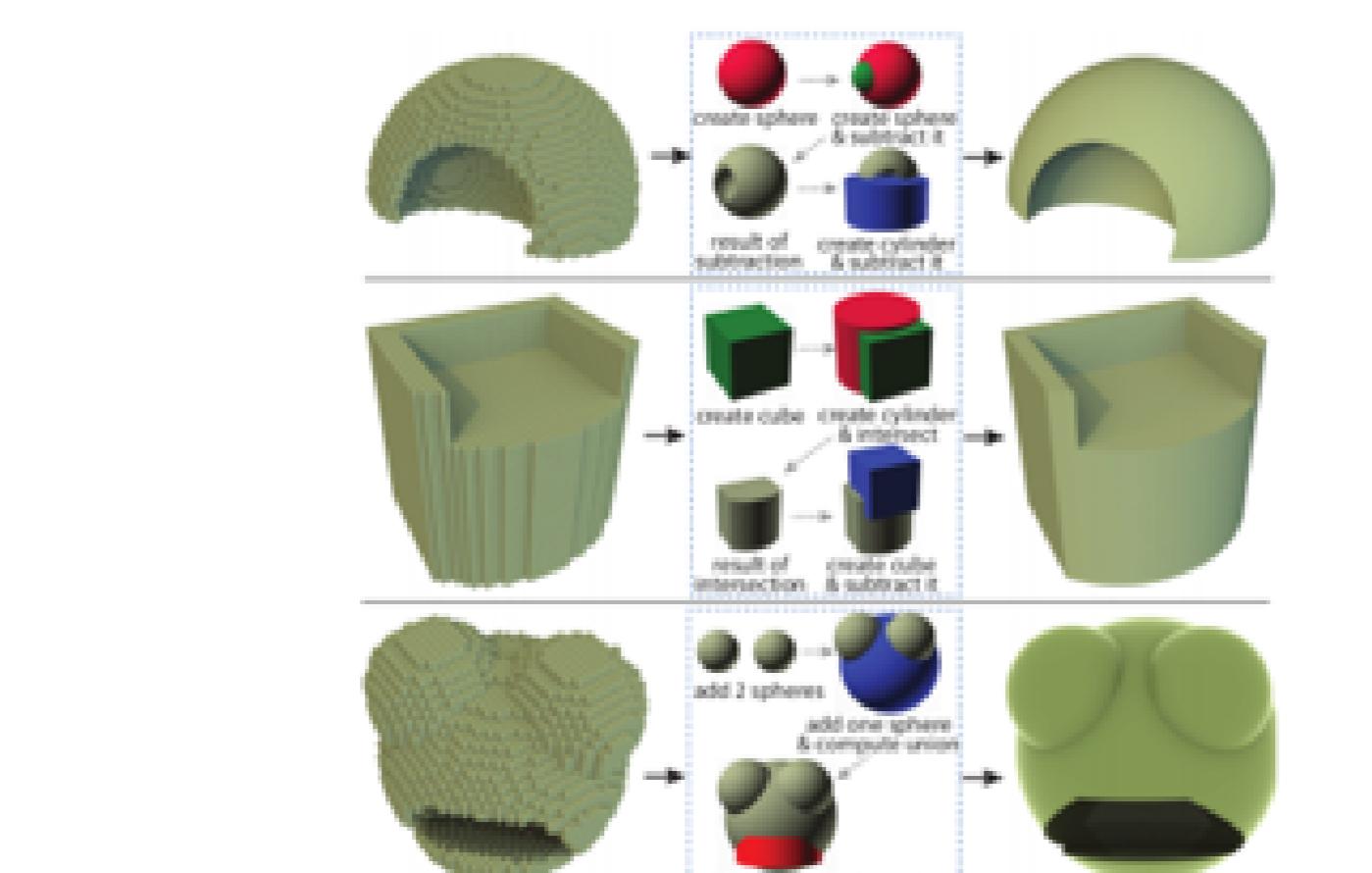
Existing approaches

Time consuming inference



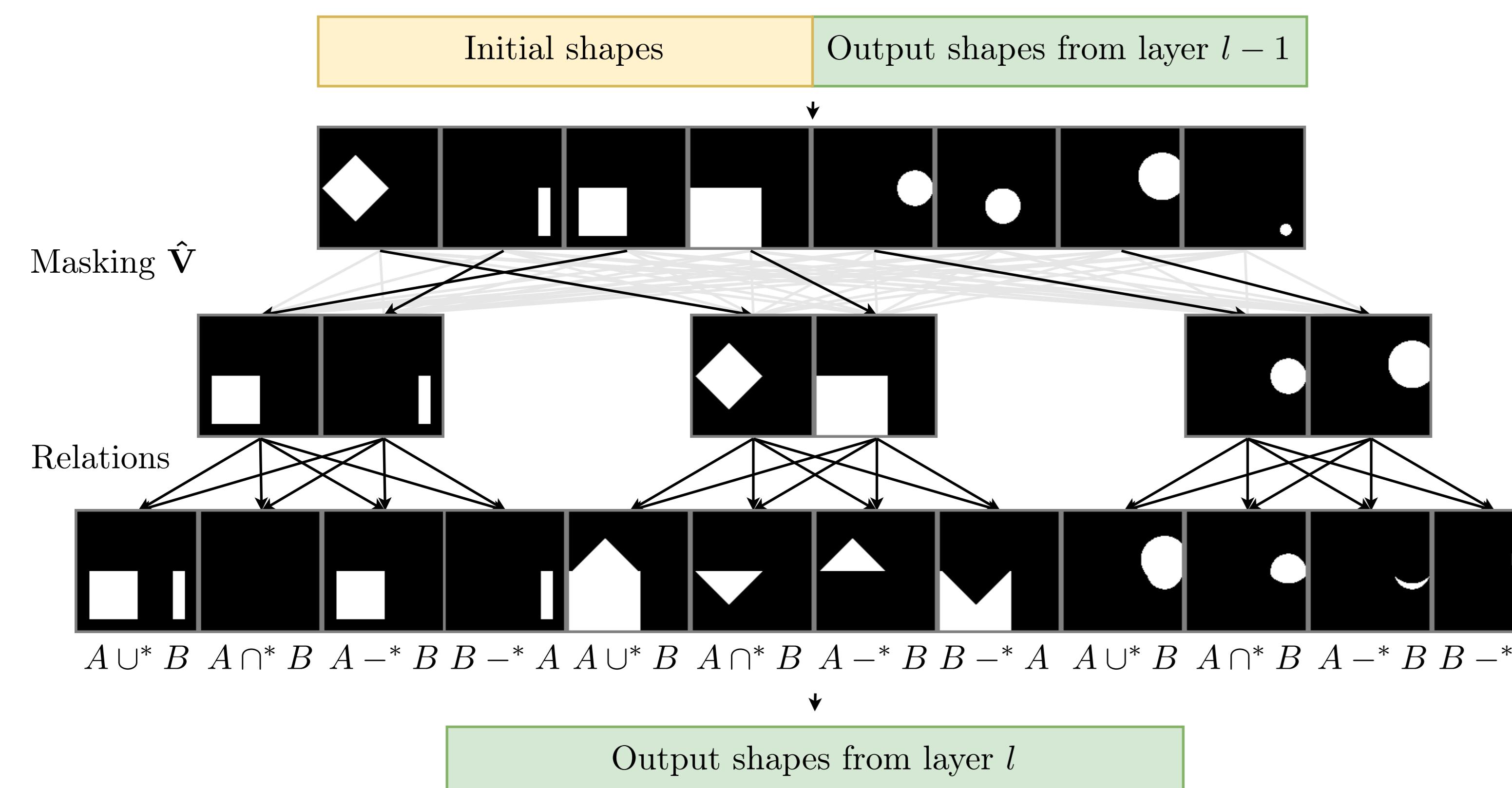
input
77 leaves
(solid primitives)
46 internal modes
(boolean operations)

Require supervision of CSG operations



CSG-Net, Sharma et al., CVPR 2018

Learnable CSG Layer



- Masks (separate for left and right operands of CSG operations) select pair of elements:

$$\mathbf{v}_{\text{left}} = \text{softmax}(\mathbf{K}_{\text{left}} \mathbf{z}) \quad \mathbf{v}_{\text{right}} = \text{softmax}(\mathbf{K}_{\text{right}} \mathbf{z})$$

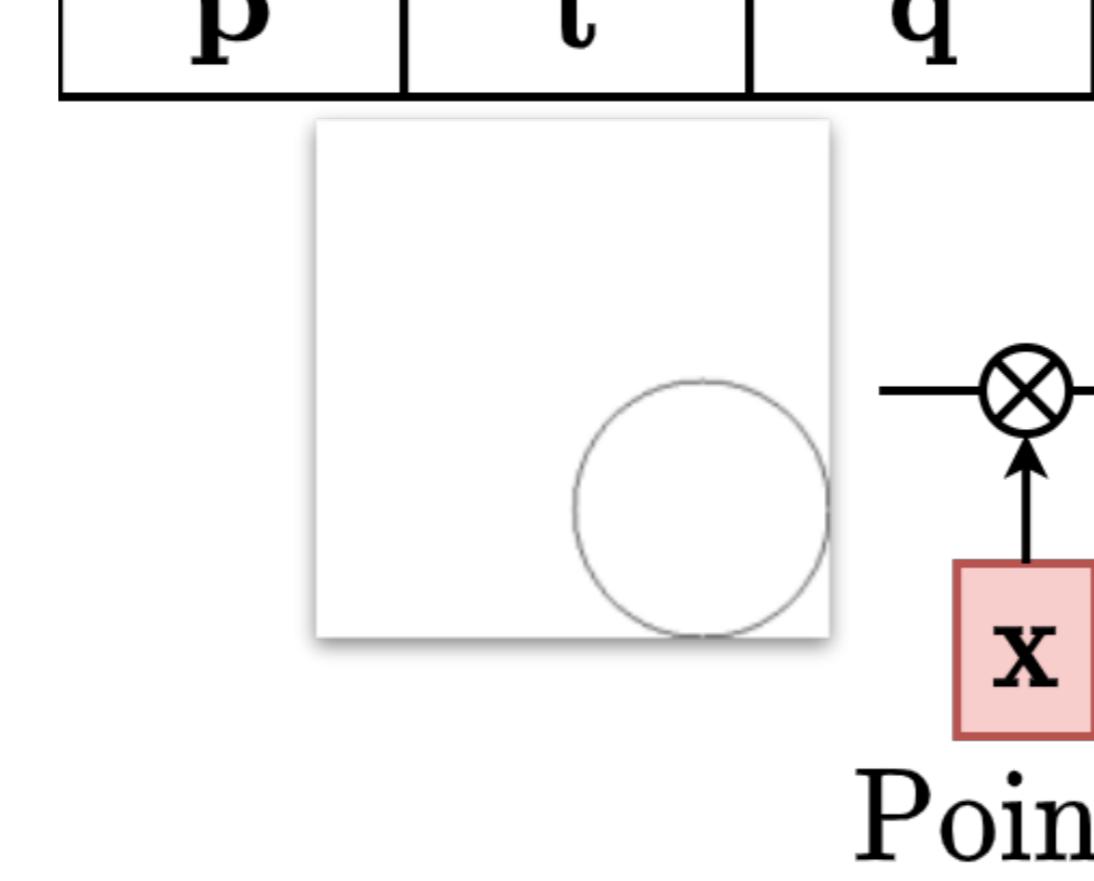
- Masked shapes $\hat{\mathbf{v}}_{\text{side},i}$ are obtained by sampling Gumbel-Softmax.

- Operands for l -th layer are obtained as:

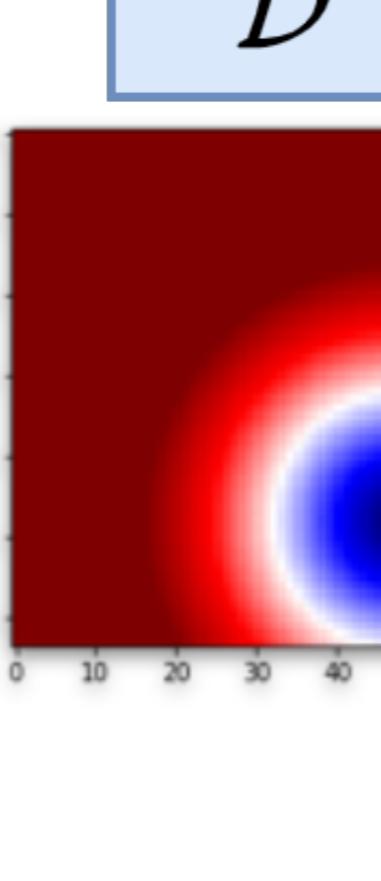
$$A = \mathcal{O}_{\text{left}} = \sum_{i=1}^M \mathcal{O}_i \hat{\mathbf{v}}_{\text{left},i} \quad B = \mathcal{O}_{\text{right}} = \sum_{i=1}^M \mathcal{O}_i \hat{\mathbf{v}}_{\text{right},i}$$

Representing a single shape and CSG operations

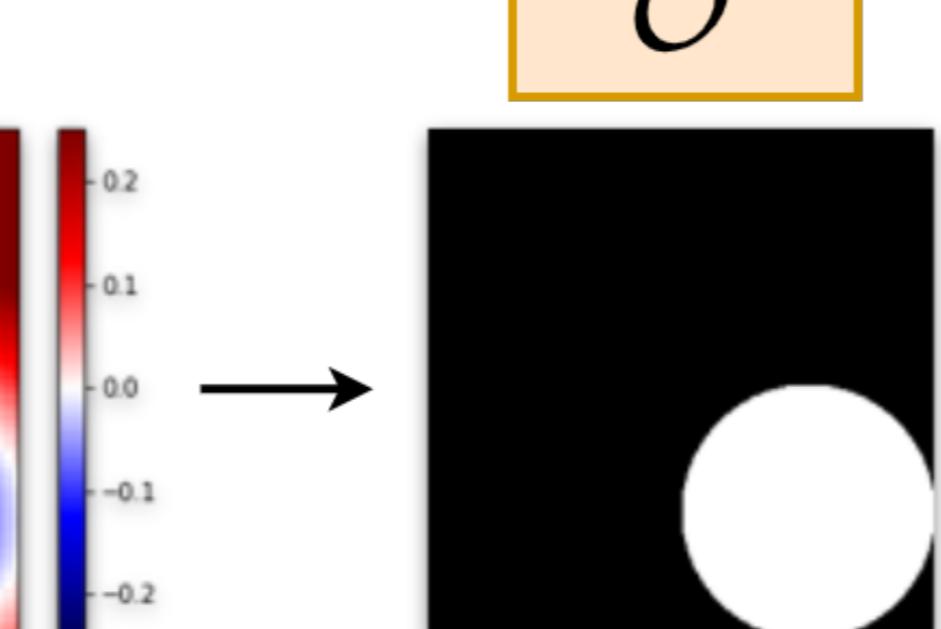
Primitive
 \mathbf{p} \mathbf{t} \mathbf{q}



SDF
 \mathcal{D}



Occupancy
 \mathcal{O}

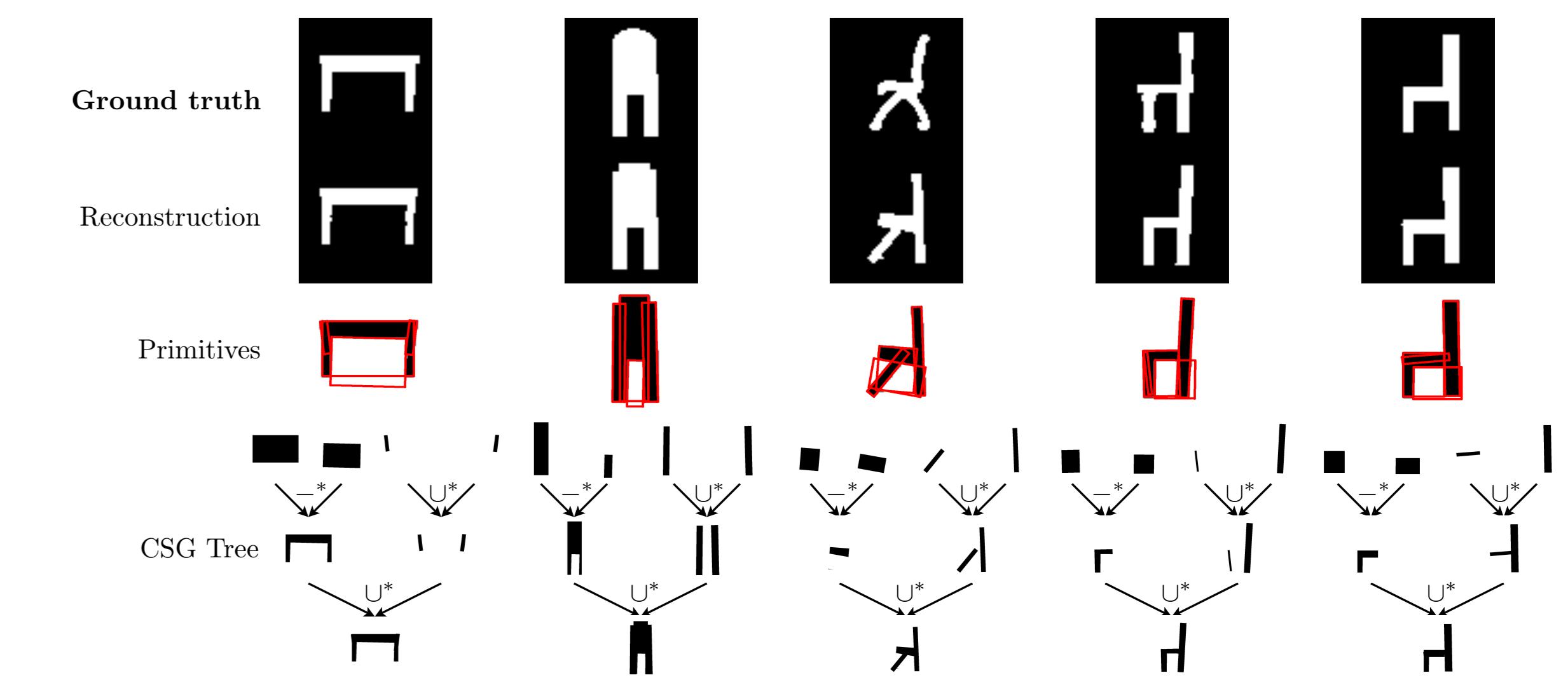


CSG operations for occupancies

$$\begin{aligned} A \cup^* B &: [\bullet + \bullet]_{[0,1]} = \bullet \\ A \cap^* B &: [\bullet + \bullet - 1]_{[0,1]} = \square \\ A -^* B &: [\bullet - \bullet]_{[0,1]} = \circ \\ B -^* A &: [\bullet - \bullet]_{[0,1]} = \circ \end{aligned}$$

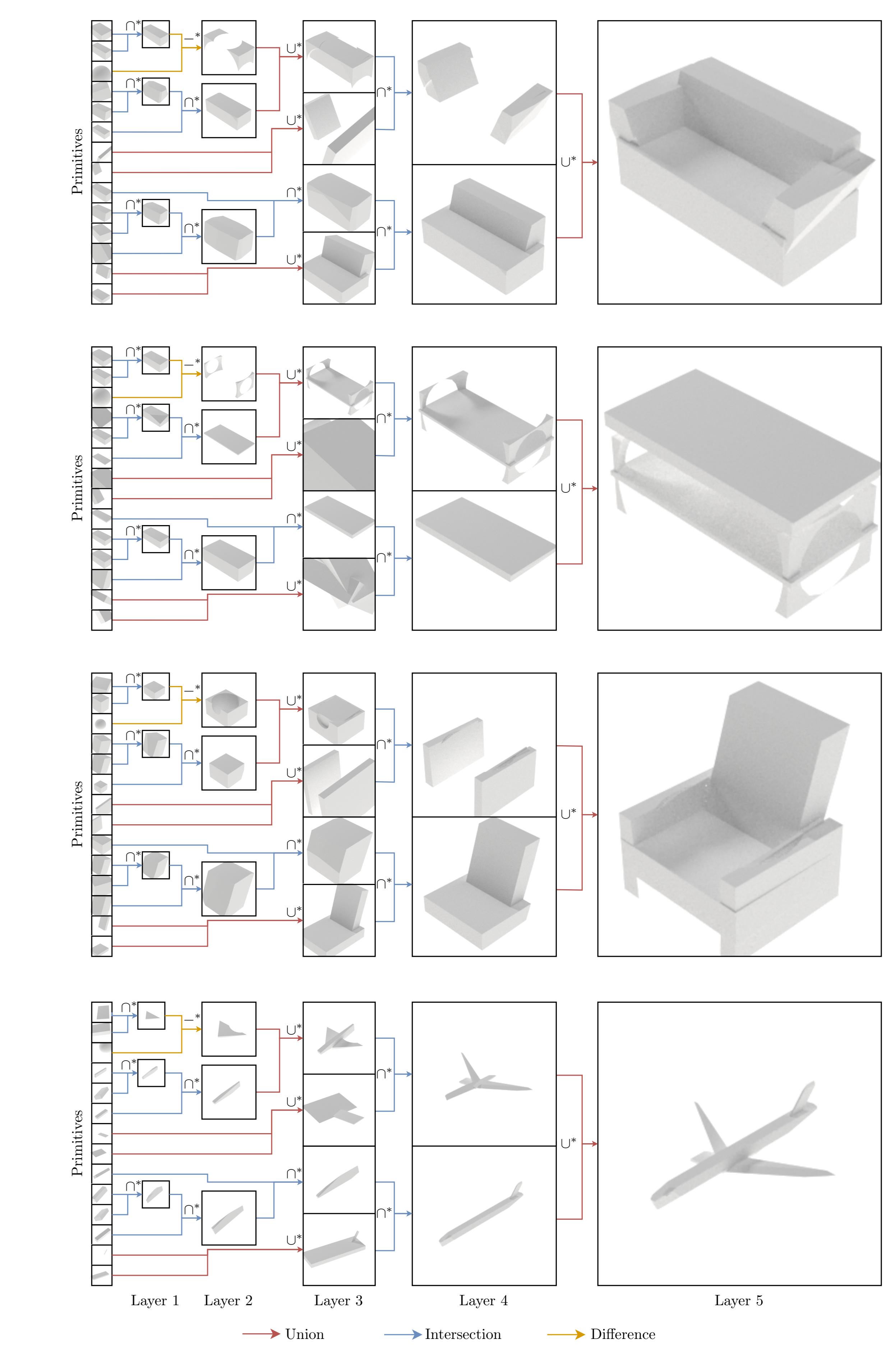
Results - 2D CAD Dataset

Method	Mode	k	$i = 0$	$i = \infty$
CSG-NETSTACK	Supervised	1	3.98	2.25
CSG-NETSTACK	Supervised	10	1.38	0.39
CSG-NETSTACK	RL	1	1.27	0.57
CSG-NETSTACK	RL	10	1.02	0.34
Our	Unsupervised	1	0.32	-



Results - 3D ShapeNet

CD - Chamfer Distance $\times 10^3$	High interpretability		Low interpretability		
	Ours	VP	SQ	BAE	BSP-Net
CD	2.085	2.259	1.656	1.592	0.446



Training UCGS-NET

$$\begin{aligned} \mathcal{L}_{\text{MSE}} &= \mathbb{E}_{\mathbf{x} \in \mathbf{X}} [(\mathcal{O}^{(L)} - \mathcal{O}^*)^2] \\ \mathcal{L}_{\text{total}} &= \underbrace{\mathcal{L}_{\text{MSE}}}_{\text{Reconstruction error}} + \underbrace{\lambda_{\mathbf{P}} \mathcal{L}_{\mathbf{P}}}_{\text{Maintain feasible parameters of primitives}} + \lambda_{\mathbf{T}} \mathcal{L}_{\mathbf{T}} + \lambda_{\alpha} |\alpha| \\ \mathcal{L}_{\mathbf{P}} &= \sum_{i=1}^M \sum_{p_i \in \mathbf{p}_i} \max(-p_i, 0) \end{aligned}$$

Second stage - when $\alpha \leq 0.05$

$$\mathcal{L}_{\text{total}}^* = \mathcal{L}_{\text{total}} + \lambda_{\tau} \sum_{l=1}^L |\tau^{(l)}|$$

Pushes CSG operations towards one-hot vectors